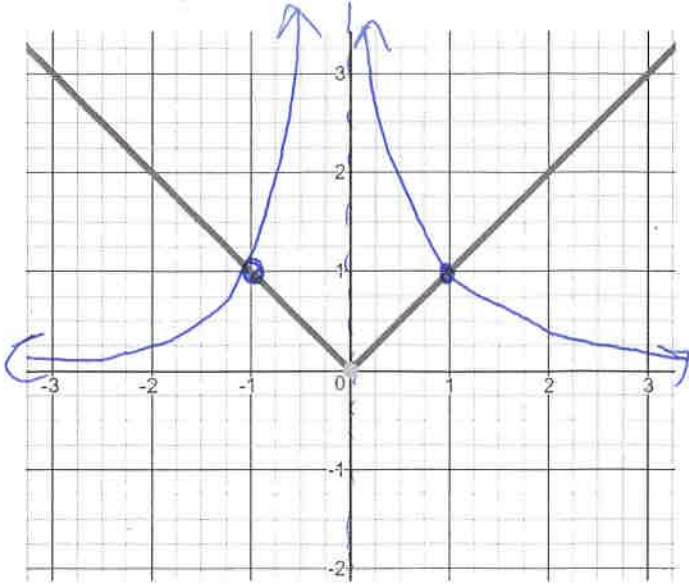
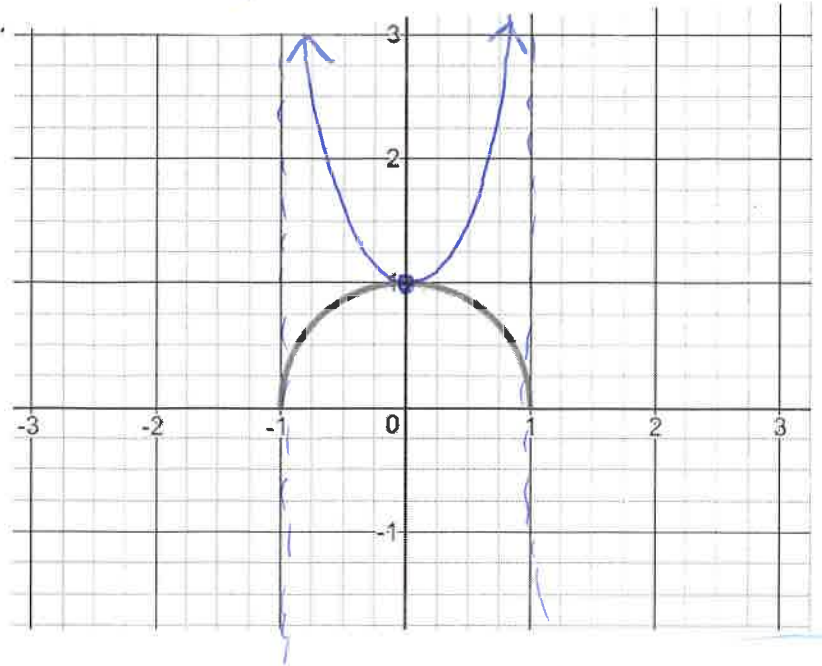


1. a)



$x=0$

b)

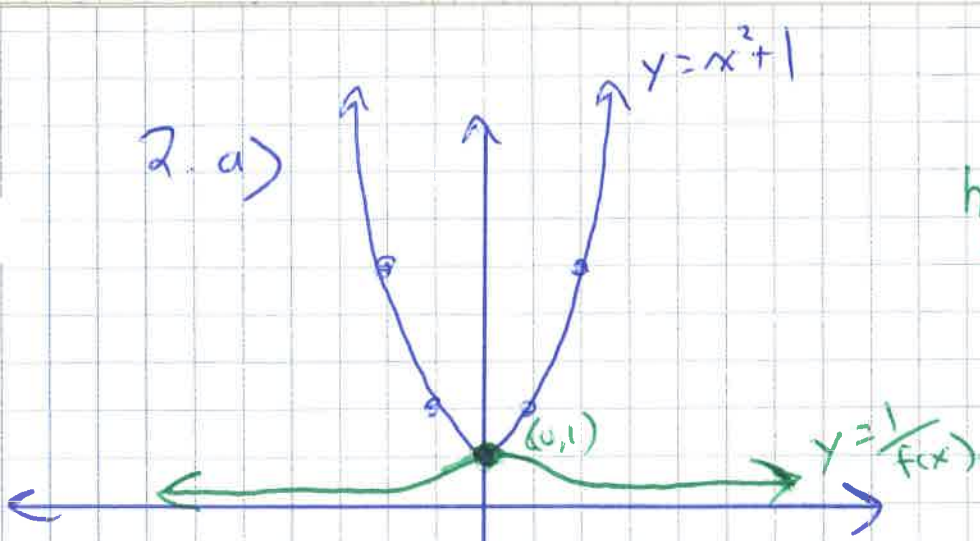


$x=-1$

$x=1$

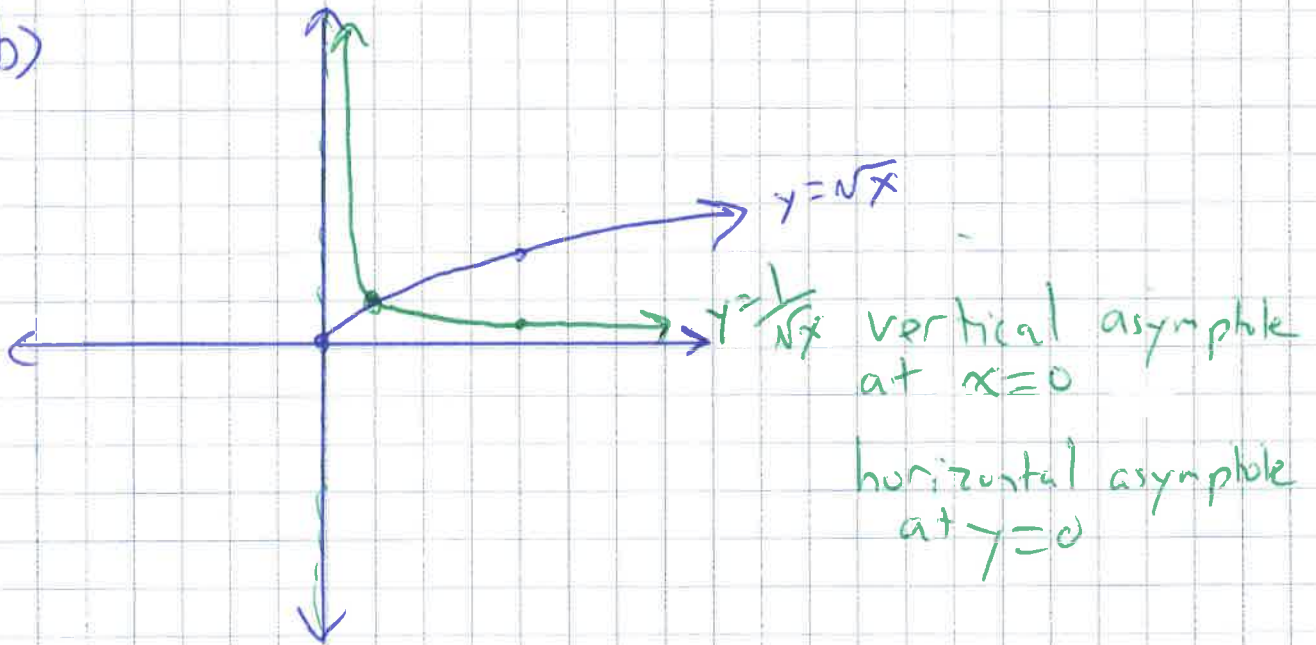
(#2 on next page).

2. a)



horizontal asymptote at  $y = 0$

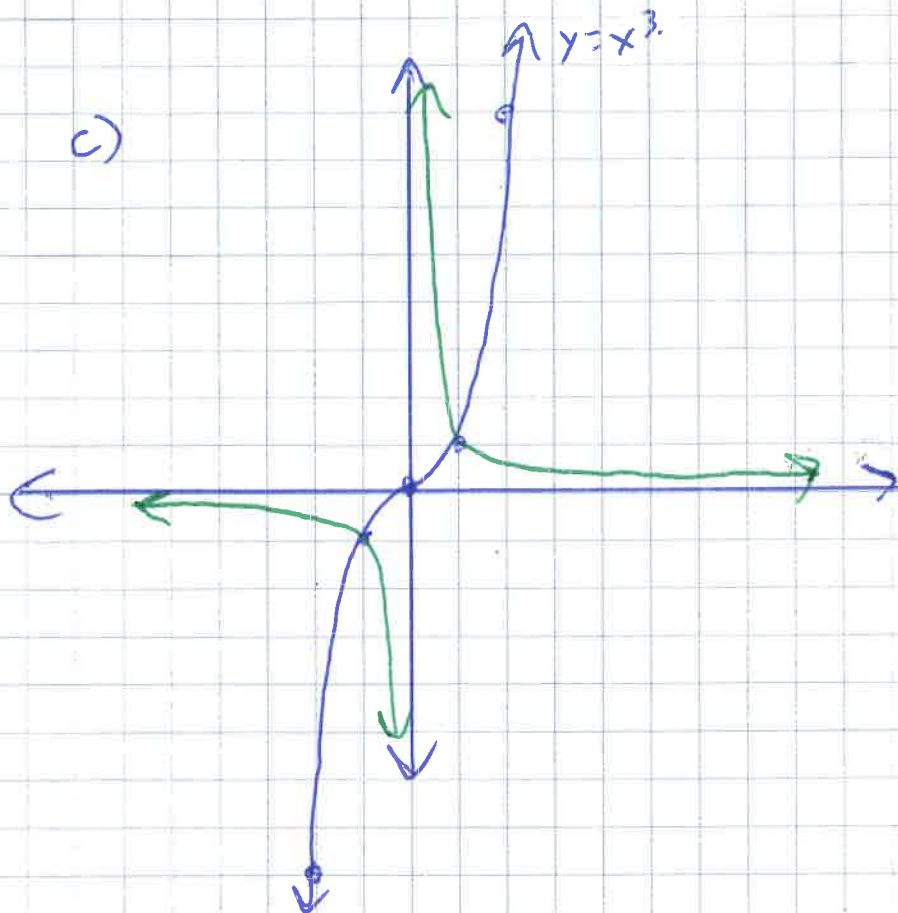
b)



vertical asymptote at  $x = 0$

horizontal asymptote at  $y = 0$

c)



vertical asymptote at  $x=0$

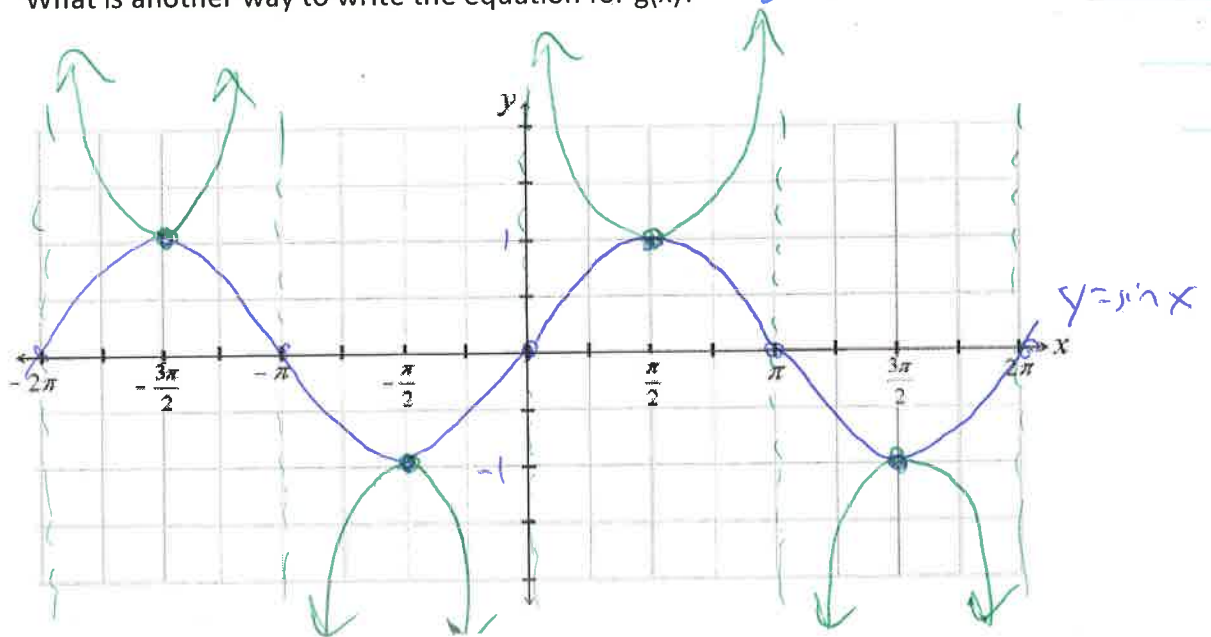
horizontal asymptote at  $y=0$ .

3. Let  $f(x) = \sin x$  (with  $x$  in radians, of course!!!)

a) Sketch 2 cycles of the graph of  $f(x)$  below.

b) Let  $g(x) = \frac{1}{\sin x}$ . Sketch  $g(x)$  below as well.

c) What is another way to write the equation for  $g(x)$ ?



$$4. f(x) = x^3 - x^2 - x + 1$$

$$\lim_{x \rightarrow \pm \infty} f(x) = \pm \infty$$

$$f(0) = 1$$

$$0 = x^3 - x^2 - x + 1$$

$$0 = x^2(x-1) - (x-1)$$

$$0 = (x-1)(x^2-1)$$

$$0 = (x-1)(x-1)(x+1)$$

$$0 = (x-1)^2(x+1)$$

x-inter at  $x=1$  and  $x=-1$ .

$$f'(x) = 3x^2 - 2x - 1$$

$$f'(x) = 0 \rightarrow \begin{aligned} 0 &= 3x^2 - 2x - 1 \\ 0 &= (3x+1)(x-1) \end{aligned}$$

$$f\left(-\frac{1}{3}\right) = \left(-\frac{1}{3}\right)^3 - \left(-\frac{1}{3}\right)^2 + \frac{1}{3} + 1 \quad \begin{array}{l} x = -\frac{1}{3} \\ x = 1 \\ (1, 0) \end{array}$$

$$\begin{aligned} f\left(-\frac{1}{3}\right) &= -\frac{1}{27} - \frac{1}{9} + \frac{1}{3} + 1 \\ &= -\frac{1}{27} - \frac{3}{27} + \frac{9}{27} + \frac{27}{27} \\ &= \frac{23}{27} \end{aligned}$$

critical points are  $\left(-\frac{1}{3}, \frac{23}{27}\right)$  and  $(1, 0)$

both are turning points (you can check this).

