

U2/C2 HWp. 466

2. a)  $(x+2)^5$

$$\begin{aligned}
 &= x^5 + 5x^4(2) + 10x^3(2)^2 + 10x^2(2)^3 + 5x(2)^4 + (2)^5 \\
 &= x^5 + 10x^4 + 40x^3 + 80x^2 + 80x + 32
 \end{aligned}$$

b)  $(x-1)^6$

$$\begin{aligned}
 &= x^6 + 6x^5(-1)^1 + 15x^4(-1)^2 + 20x^3(-1)^3 + 15x^2(-1)^4 + 6x(-1)^5 + (-1)^6 \\
 &= x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1
 \end{aligned}$$

c)  $(2x-3)^3$

$$\begin{aligned}
 &= (2x)^3 + 3(2x)^2(-3)^1 + 3(2x)(-3)^2 + (-3)^3 \\
 &= 8x^3 - 36x^2 + 54x - 27
 \end{aligned}$$

4. a)  $(k+3)^4$

$$\begin{aligned}
 &= k^4 + 4k^3(3)^1 + 6k^2(3)^2 + 4k(3)^3 + (3)^4 \\
 &= k^4 + 12k^3 + 54k^2 + 108k + 81
 \end{aligned}$$

b)  $(y-5)^6$

$$\begin{aligned}
 &= y^6 + 6y^5(-5)^1 + 15y^4(-5)^2 + 20y^3(-5)^3 + 15y^2(-5)^4 + 6y(-5)^5 + (-5)^6 \\
 &= y^6 - 30y^5 + 375y^4 - 2500y^3 + 9375y^2 - 18750y + 15625
 \end{aligned}$$

c)  $(3q-4)^4$

$$\begin{aligned}
 &= (3q)^4 + 4(3q)^3(-4) + 6(3q)^2(-4)^2 + 4(3q)(-4)^3 + (-4)^4 \\
 &= 81q^4 - 432q^3 + 864q^2 - 768q + 256
 \end{aligned}$$

d)  $(2x+7y)^3$

$$\begin{aligned}
 &= (2x)^3 + 3(2x)^2(7y) + 3(2x)(7y)^2 + (7y)^3 \\
 &= 8x^3 + 84x^2y + 294xy^2 + 343y^3
 \end{aligned}$$

e)  $(2z^3-3y^2)^5$

$$\begin{aligned}
 &= (2z^3)^5 + 5(2z^3)^4(-3y^2)^1 + 10(2z^3)^3(-3y^2)^2 + 10(2z^3)^2(-3y^2)^3 + 5(2z^3)(-3y^2)^4 + (-3y^2)^5 \\
 &= 32z^{15} - 240z^{12}y^2 + 720z^9y^4 - 1080z^6y^6 + 810z^3y^8 - 243y^{10}
 \end{aligned}$$

5.a)

1	9	36	84	126	126	84	36	9
1	10	45	120	210				
1	11	55	165					
1	12	66						
1	13	78						

Note the pattern

↑ 9  
↑ 10  
↑ 11  
↑ 12  
↑ 13

$$(x-2)^{13}$$

$$= x^{13} + 13x^{12}(-2) + 78x^{11}(-2)^2$$

=  $x^{13} - 26x^{12} + 312x^{11}$  are the first 3 terms

$$10. \quad (3x-5y)^6$$

$$= (3x)^6 + 6(3x)^5(-5y)^1 + 15(3x)^4(-5y)^2 + 20(3x)^3(-5y)^3 + 15(3x)^2(-5y)^4 + 6(3x)(-5y)^5 + (-5y)^6$$

$$= 729x^6 - 7290x^5y + 30375x^4y^2 - 67500x^3y^3 + 84375x^2y^4 - 56250xy^5 + 15625y^6$$