

4.c)  $4a(a+1) - 3(a+1) = (4a-3)(a+1)$

5. a)  $x^2 - 5x - 14 = (x-7)(x+2)$

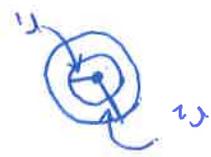
d)  $2y^2 + 5y - 7 = (2y+7)(y-1)$

7.a)  $ax + ay + bx + by = a(x+y) + b(x+y) = (a+b)(x+y)$

9.a)  $2x(x-3) + 7(3-x) = 2x(x-3) - 7(x-3) = (2x-7)(x-3)$

c)  $x^3 - x^2 - 4x + 4 = x^2(x-1) - 4(x-1) = (x^2-4)(x-1) = (x+2)(x-2)(x-1)$

12. (b)  $A = \pi(r_2^2) - \pi(r_1^2) = \pi(r_2^2 - r_1^2) = \pi(r_2 - r_1)(r_2 + r_1)$



(i)  $A = \pi(r_3 - r_1)(r_3 + r_1)$

(ii)  $D_5 = \pi(r_2^2 - r_1^2) = \pi(r_2 - r_1)(r_2 + r_1)$

(iii) Diff.  $= \pi(r_3 - r_2) - \pi(r_2 - r_1) = \pi(r_3 - r_2 - r_2 + r_1) = \pi(r_3 - r_2 - r_2 + r_1)$

$= \pi(r_3 - r_2 - r_2 + r_1) = \pi(r_3 - 2r_2 + r_1)$

f)  $12m^3 - 14m^2 - 30m + 35 = 2m^2(6m-7) - 5(6m-7) = (2m^2-5)(6m-7)$

b)  $xy + 6x + 5y + 30 = x(y+6) + 5(y+6) = (x+5)(y+6)$

b)  $2ab + 2a - 3b - 3 = 2a(b+1) - 3(b+1) = (2a-3)(b+1)$

c)  $x^3 + x^2 - x - 1 = x^2(x+1) - (x+1) = (x^2-1)(x+1) = (x-1)(x+1)^2$

$= 2(2x+5)(4x+9)$

f)  $16x^2 + 76x + 90 = 2(8x^2 + 38x + 45) = 2[2x(4x+9) + 5(4x+9)] = 2(2x+5)(4x+9)$

e)  $8a^2 - 2ab - 21b^2 = 4a(2a+3b) - 7b(2a+3b) = (4a-7b)(2a+3b)$

c)  $6m^2 - 90m + 324 = 6(m^2 - 15m + 54) = 6(m-6)(m-9)$

b)  $x^2 + 4xy - 5y^2 = (x+5y)(x-y)$

d)  $7x^2(x+1) - x(x+1) + 6(x+1) = (7x^2 - x + 6)(x+1)$

# Handout

4. d)  $\pi r^2 + \pi r h$   
 $= \pi r (r+h)$

e)  $x(2x-1) + 2(2x-1)$   
 $= (x+2)(2x-1)$

f)  $(x+3)^2 - 3(x+3)$   
 $= (x+3)(x+3-3)$   
 $= x(x+3)$

Not Assigned until next day (For L4)

5) d)  $25 - x^2 y^2$   
 $= (5-xy)(5+xy)$

\* e)  $(x+3)^2 - 16$   
 $= (x+3+4)(x+3-4)$   
 $= (x+7)(x-1)$

c)  $81x^2 - 4y^2$   
 $= (9x-2y)(9x+2y)$

f)  $(2x+3)^2 - (x-2)^2$   
 $= [2x+3-(x-2)][2x+3+(x-2)]$   
 $= (x+5)(3x+1)$

g)  $x^3 - x$   
 $= x(x^2-1)$   
 $= x(x+1)(x-1)$

h)  $\pi R^2 - \pi r^2$   
 $= \pi(R^2 - r^2)$   
 $= \pi(R+r)(R-r)$

i)  $x^4 - y^4$   
 $= (x^2+y^2)(x^2-y^2)$   
 $= (x^2+y^2)(x+y)(x-y)$

6. c)  $x^2 + 15x + 54$   
 $= (x+9)(x+6)$

f)  $x^2 - 16x - 80$   
 $= (x-20)(x+4)$

h)  $x^4 - 18x^2 + 81$   
 $= (x^2-9)^2$   
 $= (x^2-9)(x^2-9)$   
 $= (x+3)^2(x-3)^2$

i)  $x^2 + 6xy - 7y^2$   
 $= (x+7y)(x-y)$

7. b)  $12x^2 - 5x - 2$   
 $= 12x^2 + 3x - 8x - 2$   
 $= 3x(4x+1) - 2(4x+1)$   
 $= (3x-2)(4x+1)$

d)  $9x^2 - 30x + 25$   
 $= (3x-5)^2$

e)  $4x^4 - 3x^2 - 1$   
 $= (4x^2+1)(x^2-1)$   
 $= (4x^2+1)(x+1)(x-1)$

h)  $4x^4 - 13x^2 + 9$   
 $= (4x^2-9)(x^2-1)$   
 $= (2x+3)(2x-3)(x+1)(x-1)$

k)  $21x^2 - 29x + 10$   
 $= (3x-2)(7x-5)$

1	3	7	21	1	2
21	7	3	1	10	5

Sum of 29

8. a)  $x^3 - 4x^2 + 3x - 12$   
 $= x^2(x-4) + 3(x-4)$   
 $= (x^2+3)(x-4)$

b)  $2x^3 - 6x^2 - 3x + 9$   
 $= 2x^2(x-3) - 3(x-3)$   
 $= (2x^2-3)(x-3)$

c)  $4x^3 + 8x^2 - x - 2$   
 $= 4x^2(x+2) - (x+2)$   
 $= (4x^2-1)(x+2)$   
 $= (2x+1)(2x-1)(x+2)$

d)  $2x^3 - 6x^2 + 10x - 30$   
 $= 2(x^3 - 3x^2 + 5x - 15)$   
 $= 2[x^2(x-3) + 5(x-3)]$   
 $= 2(x^2+5)(x-3)$

e)  $3x^5 - 12x^3 - x^2 + 4$   
 $= 3x^3(x^2-4) - (x^2-4)$   
 $= (3x^3-1)(x^2-4)$   
 $= (3x^3-1)(x+2)(x-2)$

f)  $2x^4 - 4x^3 - 8x^2 + 16x$   
 $= 2x[x^3 - 2x^2 - 4x + 8]$   
 $= 2x[x^2(x-2) - 4(x-2)]$   
 $= 2x(x^2-4)(x-2)$   
 $= 2x(x+2)(x-2)^2$

9. a)  $x^2 - 13x + 22$   
 $= (x-11)(x-2)$

9. g)  $4x^2 + 20x + 25$   
 $= (2x+5)^2$

d)  $10x^3 - 21x^2 + 8x$   
 $= x(10x^2 - 21x + 8)$   
 $= x(10x^2 - 5x - 16x + 8)$   
 $= x[5x(2x-1) - 8(2x-1)]$   
 $= x(5x-8)(2x-1)$

9. j)  $100a^2 - 36b^2$   
 $= 4(25a^2 - 9b^2)$   
 $= 4(5a+3b)(5a-3b)$