

Function Notation

Suppose we want to define a quadratic function.

OLD Method: $y = x^2 + 3x - 4$

OLD Method:

Find the y-value of $y = x^2 + 3x - 4$ when x is equal to 3

$$\begin{aligned} y &= (3)^2 + 3(3) - 4 \\ y &= 9 + 9 - 4 \\ y &= 14 \quad \text{when } x = 3 \\ &\quad (3, 14) \end{aligned}$$

NEW Method: $f(x) = x^2 + 3x - 4$

NEW Method:

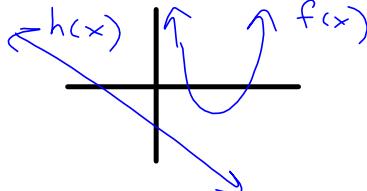
Find $f(3)$

$$\begin{aligned} f(3) &= 3^2 + 3(3) - 4 \\ f(3) &= 9 + 9 - 4 \\ f(3) &= 14 \end{aligned}$$

Besides using $f(x)$ we could also name functions $g(x)$, $h(x)$, $P(n)$, $V(t)$ etc.

Very useful for working with several functions at once. Also useful for graphing.

$$\begin{aligned} f(x) &= 3x - 1 \\ g(x) &= \frac{1}{4}x + 3 \end{aligned}$$



Example: Let $f(x) = 2x - 3$

Evaluate or simplify the following:

a) $f(-2)$	b) $f(0)$	c) $f(2a)$
$f(-2) = 2(-2) - 3$	$f(0) = 2(0) - 3$	$f(2a) = 2(2a) - 3$
$f(-2) = -7$	$f(0) = -3$	$= 4a - 3$

Example: Erika works at an electronics store and is payed every week according to the equation $E(s) = 0.032s + 300$, where $E(s)$ is her earnings based on s sales in dollars.

a) Evaluate $E(4000)$ and interpret its meaning.

$$\begin{aligned} E(4000) &= 0.032(4000) + 300 \\ &= 428 \end{aligned}$$

so she earns \$428 for
\$4000 sales

b) When does $E(s) = 600$?

$$\begin{aligned} 0.032s + 300 &= 600 \\ 0.032s &= 300 \\ \hline 0.032 & \hline \\ s &= 9375 \end{aligned}$$

Example Let $f(x) = -2x + 3$ and $g(x) = x^2 - 3x + 2$

a) Find $g(-2)$

$$\begin{aligned} g(-2) &= (-2)^2 - 3(-2) + 2 \\ &= 4 + 6 + 2 \\ &= 12 \end{aligned}$$

c) Find $2f(-1) + 3g(2)$

$$\begin{aligned} &= 2(-2(-1)+3) + 3(2^2 - 3(2) + 2) \\ &= 2(5) + 3(0) \\ &= 10 \end{aligned}$$

e) When is $f(x) = 5$?

$$\begin{aligned} -2x + 3 &= 5 \\ -2x &= 5 - 3 \\ -2x &= 2 \\ x &= 1 \end{aligned}$$

Example The graph represents a function $f(x)$.

a) Find $f(-2)$

$$= -5$$

b) Find $f(0)$. What is this point called?

$$= -4 \quad (0, -4) \quad y\text{-intercept}$$

c) When does $f(x) = 0$? What is this point called?

$$\begin{array}{lll} <-1, 0> & (1, 0) & (-4, 0) \\ x = -1, x = 1, x = -4 \end{array}$$

x -intercepts or zeroes

b) Find $f\left(\frac{3}{4}\right)$

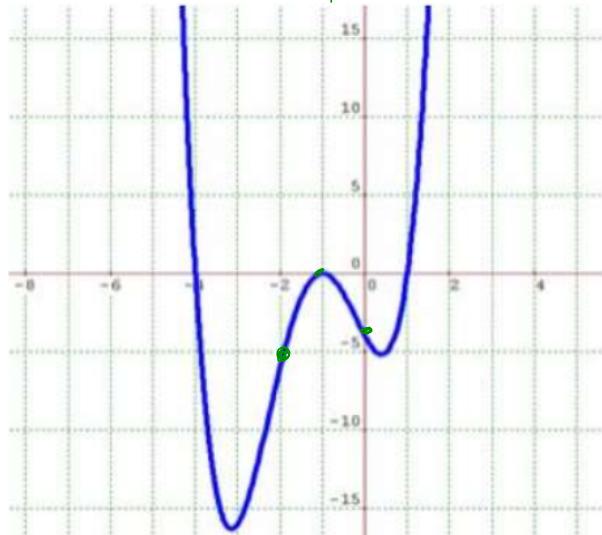
$$\begin{aligned} f\left(\frac{3}{4}\right) &= -2\left(\frac{3}{4}\right) + 3 \\ &= -\frac{6}{4} + 3 \end{aligned}$$

d) Find $f(g(4))$

$$\begin{aligned} g(4) &= 4^2 - 3(4) + 2 = \frac{3}{2} + 3 \\ &= 16 - 12 + 2 = \frac{3}{2} \\ g(4) &= 6 \end{aligned}$$

$$f(g(4)) = f(6)$$

$$\begin{aligned} &= -2(6) + 3 \\ &= -9 \end{aligned}$$



* Never do this.

$$\begin{aligned} g(x) &= 3x^2 - 2 \\ g(2) &= 3x^2 - 2 \quad \cancel{x} \\ g(2) &= 3(2)^2 - 2 \quad \cancel{2} \end{aligned}$$

$$= 10$$

OR This:

$$\begin{aligned} g(x) &= 3x^2 - 2 \\ g(x) &= 3(2)^2 - 2 \\ &= 10 \end{aligned}$$

Text page 13 #8 – 11, 16

and page 54 #2 - 3