

MCF3M

Graphing Parabolas of the Form $y = (x - h)^2$

Equation: $y = (x + 2)^2$

$h = -2$

x	y
-4	4
-3	1
-2	0
-1	1
0	4
1	9
2	16

Vertex: $(-2, 0)$ **Zeros:** -2

Step Pattern: $1, 3, 5, 7, \dots$

Direction of Opening: \cup

Equation: $y = (x - 1)^2$

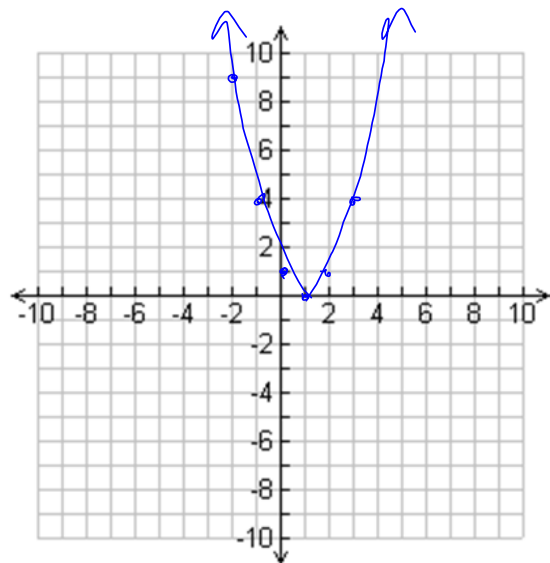
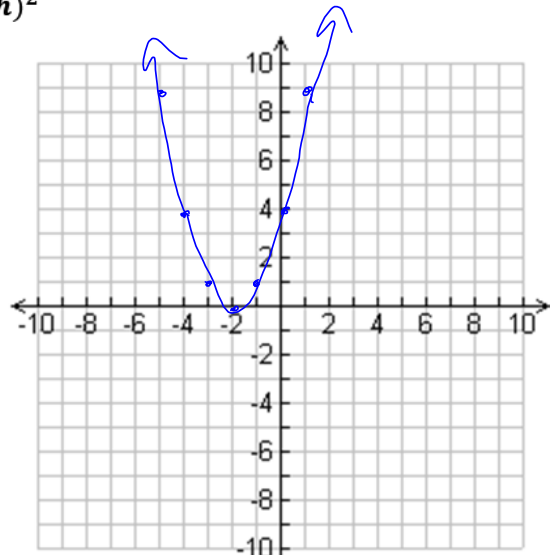
$h = 1$

x	y
-3	16
-2	9
-1	4
0	1
1	0
2	1
3	4

Vertex: $(1, 0)$ **Zeros:** 1

Step Pattern: $1, 3, 5, 7, \dots$

Direction of Opening: \cup



Summary

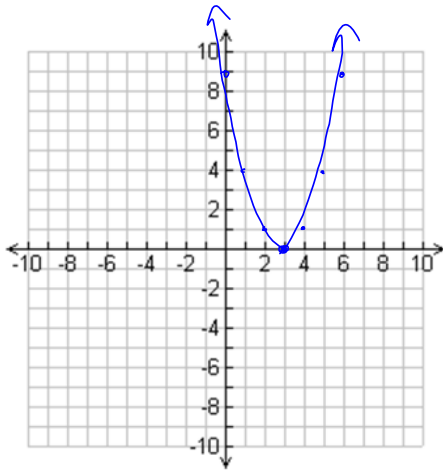
The graph of $y = (x - h)^2$ is the graph of $y = x^2$ shifted to right/left h units.

The step pattern will be $1, 3, 5, 7, \dots$. The vertex will be at $(h, 0)$.

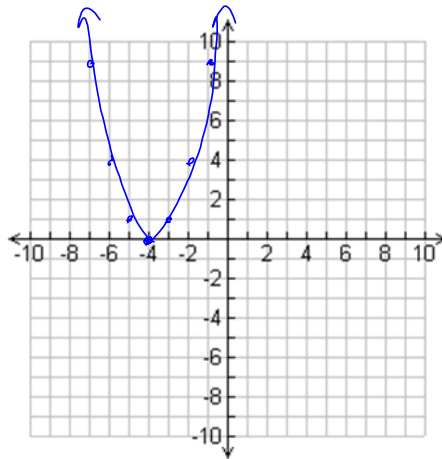
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Sketch each graph below without making a table of values.

$$y = (x - 3)^2$$



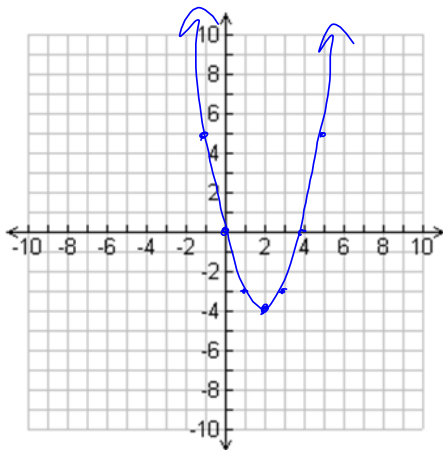
$$y = (x + 4)^2$$



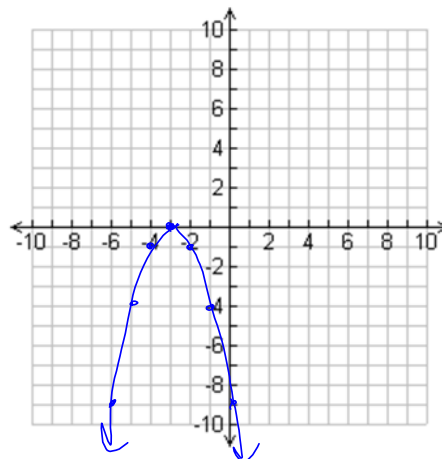
How about combining a couple of transformations? Try to graph the following without making a table of values. Check at least one point on your graph with the equation.

$$y = (x - 2)^2 - 4$$

$$(2, -4)$$



$$y = -(x + 3)^2$$



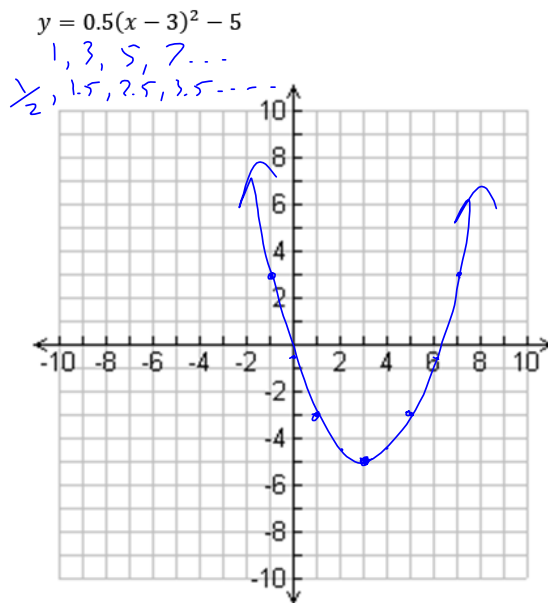
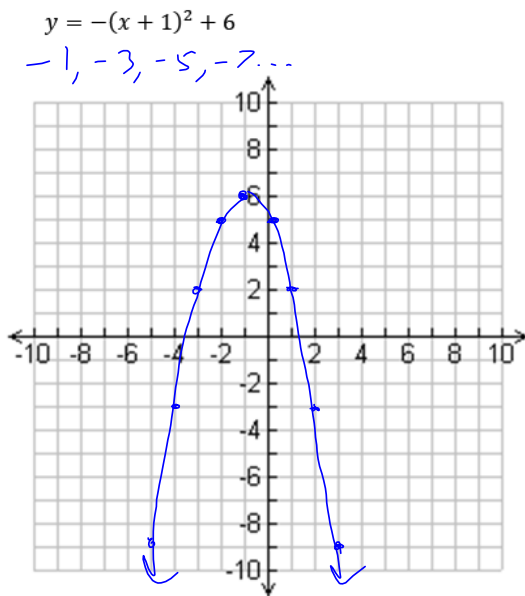
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Putting it All Together – The Vertex Form of a Parabola


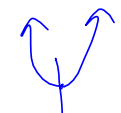
We can combine everything we have learned over the last 3 lessons to graph any quadratic relationship with an equation of the form $y = a(x - h)^2 + k$.

To graph quadratic equations in this form, start with the graph of $y = x^2$ and:

Examples Sketch each of the following. Describe the transformations below the graph.



Why do you think the $y = a(x - h)^2 + k$ is referred to as *vertex form*?

 $y = 3(x - 4)^2 + 10$ (4, 10) $\{y \in \mathbb{R} \mid y \geq 10\}$	$y = -(x + 4)^2 - 1$ (-4, -1) $\{y \in \mathbb{R} \mid y \leq -1\}$	at $y = 3x^2 + 12$ (0, 12) $\{y \in \mathbb{R} \mid y \geq 12\}$	
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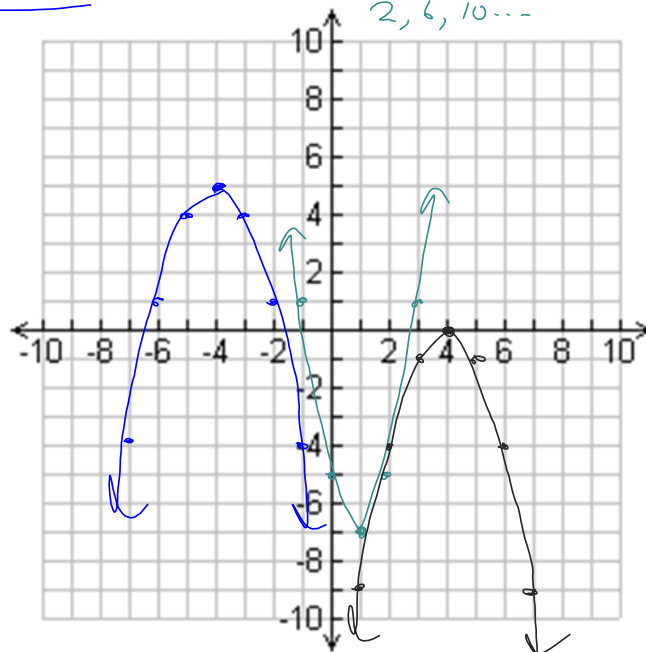
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Graph the following.

$y = -(x + 4)^2 + 5$

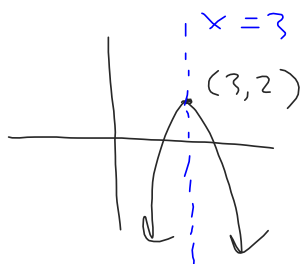
$y = 2(x - 1)^2 - 7$
2, 6, 10...

$y = -(x - 4)^2$
1, 3, 5, ...



Draw a very rough sketch of the parabola below. State the max/min value, the vertex and the axis of symmetry. $x = 3$

$y = -4(x - 3)^2 + 2$



$y \leq 2$ (3, 2)
 $y = 2$ is a maximum

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